1. This is pretty much a contrapositive of the theorem. Suppose that $f$ has a constant value throughout some neighborhood contained in $D$. Since a neighborhood is a domain, the theorem implies that $f$ is constant throughout $D$, in contradiction to our assumption. Thus there can be no neighborhood in $D$ on which $f$ is constant.